

Compact funcoids

Compact funcoids are defined. Attempted to prove that under certain conditions the reloid corresponding to a compact funcoid is the neighborhood of the diagonal of the product funcoid.

This is a rough partial draft. The proofs are with errors.

FiXme: The below examples also show that subatomic product does not coincide with Tychonoff product.

1. The rest

DEFINITION 2090. A funcoid f is *directly compact* iff

$$\forall \mathcal{F} \in \mathfrak{F} : (\langle f \rangle \mathcal{F} \neq \perp \Rightarrow \text{Cor} \langle f \rangle \mathcal{F} \neq \perp).$$

OBVIOUS 2091. A funcoid f is directly compact iff $\forall a \in \text{atoms dom } f : \text{Cor} \langle f \rangle a \neq \perp$.

OBVIOUS 2092. A reflexive funcoid f is directly compact iff

$$\forall \mathcal{F} \in \mathfrak{F} : (\mathcal{F} \neq \perp \Rightarrow \text{Cor} \langle f \rangle \mathcal{F} \neq \perp).$$

DEFINITION 2093. A funcoid f is *reversely compact* iff f^{-1} is directly compact.

DEFINITION 2094. A funcoid is *compact* iff it is both directly compact and reversely compact.

PROPOSITION 2095. $\prod^{\text{RLD}} a = \uparrow^{\text{RLD}} \prod_{i \in \text{dom } a} (\uparrow^{\text{RLD}})^{-1} a_i$ for every indexed family a of principal filters.

PROOF. Because $\prod_{i \in \text{dom } a} (\uparrow^{\text{RLD}})^{-1} a_i \in \text{up } \prod^{\text{RLD}} a$. **FiXme:** More detailed proof. \square

LEMMA 2096. $\prod_{i \in \text{dom } a}^{\text{RLD}} \text{Cor } a_i = \text{Cor } \prod^{\text{RLD}} a$.

PROOF. $\text{Cor } \prod^{\text{RLD}} a = \prod \{ \uparrow^{\text{RLD}} \prod A \mid A \in \text{up } a \} = \uparrow^{\text{RLD}} \bigcap \{ \prod A \mid A \in \mathscr{P} \prod \mathfrak{A}, \forall i \in \text{dom } a : A_i \in \text{up } a_i \} = \uparrow^{\text{RLD}} \bigcap \{ \prod \bigcap K_i \mid K \in \mathscr{P} \mathscr{P} \prod \mathfrak{A}, \forall i \in \text{dom } a : K_i \in \mathscr{P} \text{up } a_i \} = \uparrow^{\text{RLD}} \bigcap \{ \prod (\uparrow^{\text{RLD}})^{-1} \text{Cor } a_i \mid i \in \text{dom } a \} = \uparrow^{\text{RLD}} \prod_{i \in \text{dom } a}^{\text{RLD}} \text{Cor } a_i$.

FiXme: Check for little errors. \square

COROLLARY 2097. $\prod_{i \in n}^{\text{RLD}} \langle \text{CoCompl } f_i \rangle \mathcal{X}_i = \langle \text{CoCompl } \prod^{(A)} f \rangle \prod^{\text{RLD}} \mathcal{X}$ for every n -indexed families f of funcoids and \mathcal{X} of filters on the same set (with $\text{Src } f_i = \text{Base}(\mathcal{X}_i)$ for every $i \in n$).