

is defined by the formulas:

$$\langle \rho f \rangle x = f \circ x \quad \text{and} \quad \langle \rho f^{-1} \rangle y = f^{-1} \circ y$$

where  $x$  are endoreloids on  $\text{Src } f$  and  $y$  are endoreloids on  $\text{Dst } f$ .

PROPOSITION 1162. It is really a functor (if we equate reloids  $x$  and  $y$  with corresponding filters on Cartesian products of sets).

PROOF.  $y \neq \langle \rho f \rangle x \Leftrightarrow y \neq f \circ x \Leftrightarrow f^{-1} \circ y \neq x \Leftrightarrow \langle \rho f^{-1} \rangle y \neq x$ .  $\square$

COROLLARY 1163.  $(\rho f)^{-1} = \rho f^{-1}$ .

DEFINITION 1164. It can be continued to arbitrary functors  $x$  having destination  $\text{Src } f$  by the formula  $\langle \rho^* f \rangle x = \langle \rho f \rangle \text{id}_{\text{Src } f} \circ x = f \circ x$ .

PROPOSITION 1165.  $\rho$  is an injection.

PROOF. Consider  $x = \text{id}_{\text{Src } f}$ .  $\square$

PROPOSITION 1166.  $\rho(g \circ f) = (\rho g) \circ (\rho f)$ .

PROOF.  $\langle \rho(g \circ f) \rangle x = g \circ f \circ x = \langle \rho g \rangle \langle \rho f \rangle x = (\langle \rho g \rangle \circ \langle \rho f \rangle) x$ . Thus  $\langle \rho(g \circ f) \rangle = \langle \rho g \rangle \circ \langle \rho f \rangle = \langle (\rho g) \circ (\rho f) \rangle$  and so  $\rho(g \circ f) = (\rho g) \circ (\rho f)$ .  $\square$

THEOREM 1167.  $\rho \sqcup F = \sqcup \langle \rho \rangle^* F$  for a set  $F$  of reloids.

PROOF. It's enough to prove  $\langle \rho \sqcup F \rangle^* X = \langle \sqcup \langle \rho \rangle^* F \rangle^* X$  for a set  $X$ . Really,

$$\begin{aligned} \langle \rho \sqcup F \rangle^* X &= \\ \langle \rho \sqcup F \rangle \uparrow X &= \\ \sqcup F \circ \uparrow X &= \\ \sqcup \left\{ \frac{f \circ \uparrow X}{f \in F} \right\} &= \\ \sqcup \left\{ \frac{\langle \rho f \rangle \uparrow X}{f \in F} \right\} &= \\ \left\langle \sqcup \left\{ \frac{\rho f}{f \in F} \right\} \right\rangle X &= \\ \left\langle \sqcup \langle \rho \rangle^* F \right\rangle^* X. & \end{aligned}$$

$\square$

CONJECTURE 1168.  $\rho \sqcap F = \sqcap \langle \rho \rangle^* F$  for a set  $F$  of reloids.

PROPOSITION 1169.  $\rho 1_A^{\text{RLD}} = 1_{\mathcal{P}(A \times A)}^{\text{FCD}}$ .

PROOF.  $\langle \rho 1_A^{\text{RLD}} \rangle x = 1_A^{\text{RLD}} \circ x = x = \left\langle 1_{\mathcal{P}(A \times A)}^{\text{FCD}} \right\rangle x$ .  $\square$

We can try to develop further theory by applying embedding of reloids into functors for researching of properties of reloids.

THEOREM 1170. Reloid  $f$  is monovalued iff functor  $\rho f$  is monovalued.