

$$\begin{aligned}
(\prod G) \circ f &= \prod \{\uparrow^{\text{RLD}}(g \circ \varphi) \mid g \in \text{xyGR} \prod G\}; \\
\text{GR} \prod \{g \circ f \mid g \in G\} &= \text{GR} \prod \{\prod \{\uparrow^{\text{RLD}}(\Gamma \circ \varphi) \mid \Gamma \in \text{xyGR} g\} \mid g \in G\} = \text{GR} \prod \cup \{\{\uparrow^{\text{RLD}}(\Gamma \circ \varphi) \mid \Gamma \in \text{xyGR} g\} \mid g \in G\} \\
&= \text{GR} \prod \{\uparrow^{\text{RLD}}(\Gamma \circ \varphi) \mid \Gamma \in \text{xyGR} \prod G\} = \{(\Gamma_0 \circ \varphi) \sqcap \dots \sqcap (\Gamma_n \circ \varphi) \mid \Gamma_i \in \cup G \text{ where } i = 0, \dots, n \text{ for } n \in \mathbb{N}\} \\
&= (\text{proposition above}) = \{(\Gamma_0 \sqcap \dots \sqcap \Gamma_n) \circ \varphi \mid \Gamma_i \in \cup G \text{ where } i = 0, \dots, n \text{ for } n \in \mathbb{N}\} = \{\Gamma \circ \varphi \mid \Gamma \in \text{xyGR} \prod G\}. \\
\text{Thus } (\prod G) \circ f &= \prod \{g \circ f \mid g \in G\}. \quad \square
\end{aligned}$$

Theorem 13.85.

1. Monovalued reloids are metamonovalued.
2. Injective reloids are metainjective.

Proof. We will prove only the first, as the second is dual.

Let G be a set of reloids and f be a monovalued reloid.

Let f' be a principal monovalued continuation of f (so that $f = f'|_{\text{dom } f}$).

By the lemma $(\prod G) \circ f' = \prod \{g \circ f' \mid g \in G\}$. Restricting this equality to $\text{dom } f$ we get:

$$(\prod G) \circ f = \prod \{g \circ f \mid g \in G\}. \quad \square$$

Conjecture 13.86. Every metamonovalued reloid is monovalued.