

3°. conforming to Wallman's disjunction property.

PROOF. By theorem 180. □

REMARK 654. For more ways to characterize (atomic) separability of the lattice of funcoids see subsections "Separation subsets and full stars" and "Atomically separable lattices".

COROLLARY 655. The lattice $\text{FCD}(A; B)$ is an atomistic lattice.

PROOF. **Fixme: Should be generalized.** Let $f \in \text{FCD}(A; B)$. Suppose contrary to the statement to be proved that $\bigsqcup \text{atoms } f \sqsubset f$. Then there exists $a \in \text{atoms } f$ such that $a \sqcap \bigsqcup \text{atoms } f = \perp^{\text{FCD}(A; B)}$ what is impossible. □

PROPOSITION 656. $\text{atoms}(f \sqcup g) = \text{atoms } f \cup \text{atoms } g$ for every funcoids $f, g \in \text{FCD}(A; B)$ (for every sets A, B).

PROOF. $a \times^{\text{FCD}} b \not\prec f \sqcup g \Leftrightarrow a [f \sqcup g] b \Leftrightarrow a [f] b \vee a [g] b \Leftrightarrow a \times^{\text{FCD}} b \not\prec f \vee a \times^{\text{FCD}} b \not\prec g$ for every atomic filters a and b . □

THEOREM 657. For every $f, g, h \in \text{FCD}(A; B)$, $R \in \mathcal{PFCD}(A; B)$ (for every sets A and B)

- 1°. $f \sqcap (g \sqcup h) = (f \sqcap g) \sqcup (f \sqcap h)$;
- 2°. $f \sqcup \bigsqcap R = \bigsqcap \langle f \sqcup \rangle^* R$.

PROOF. We will take into account that the lattice of funcoids is an atomistic lattice.

1°.

$$\begin{aligned}
 \text{atoms}(f \sqcap (g \sqcup h)) &= \\
 \text{atoms } f \cap \text{atoms}(g \sqcup h) &= \\
 \text{atoms } f \cap (\text{atoms } g \cup \text{atoms } h) &= \\
 (\text{atoms } f \cap \text{atoms } g) \cup (\text{atoms } f \cap \text{atoms } h) &= \\
 \text{atoms}(f \sqcap g) \cup \text{atoms}(f \sqcap h) &= \\
 \text{atoms}((f \sqcap g) \sqcup (f \sqcap h)). &
 \end{aligned}$$