

PROOF. By theorem 366. \square

PROPOSITION 448. $\text{Cor}' a = \text{Cor } a = \uparrow^{\text{Base}(a)} \cap a$ for every filter a on a set.

PROOF. By proposition 367. \square

PROPOSITION 449. $\text{Cor } a \sqsubseteq a$ for every filter a on a set.

PROOF. By proposition 368. \square

PROPOSITION 450. $\text{Cor } a = \max \text{down } a$ for every filter a on a set.

PROOF. By proposition 369. \square

PROPOSITION 451. For the lattice \mathfrak{F} of filters on a set \mathfrak{U} , $\mathcal{A} \in \mathfrak{F}$, $B \in \mathfrak{P}$ we have:

$$1^\circ. B \prec^{\mathfrak{F}} \mathcal{A} \Leftrightarrow \overline{B} \sqsupseteq \mathcal{A};$$

$$2^\circ. B \equiv^{\mathfrak{F}} \mathcal{A} \Leftrightarrow \overline{B} \sqsubseteq \mathcal{A}.$$

PROOF. By theorem 370. \square

PROPOSITION 452. $\bigsqcup^{\mathfrak{F}} S = \bigcap S$ for a set S of filters on a powerset.

PROOF. By theorem 373. \square

COROLLARY 453. A set of filters on a powerset is always a complete lattice.

COROLLARY 454. $\mathcal{A} \sqcup \mathcal{B} = \mathcal{A} \cap \mathcal{B}$ for filters \mathcal{A} and \mathcal{B} on a powerset.

PROPOSITION 455. For $S \in \mathcal{P}\mathfrak{F} \setminus \{\emptyset\}$ where \mathfrak{F} are filters on a powerset

$$\bigsqcup^{\mathfrak{F}} S = \left\{ \frac{K_0 \cap \dots \cap K_n}{K_i \in \bigcup S \text{ where } i = 0, \dots, n \text{ for } n \in \mathbb{N}} \right\}.$$

PROOF. By theorem 377. \square

PROPOSITION 456. For every $\mathcal{F}_0, \dots, \mathcal{F}_m$ ($m \in \mathbb{N}$) where \mathfrak{F} are filters on a powerset

$$\mathcal{F}_0 \sqcap^{\mathfrak{F}} \dots \sqcap^{\mathfrak{F}} \mathcal{F}_m = \left\{ \frac{K_0 \cap \dots \cap K_m}{K_i \in \mathcal{F}_i \text{ where } i = 0, \dots, m} \right\}.$$

PROOF. By theorem 378. \square

PROPOSITION 457. If $\mathcal{A} \in \mathfrak{F}$ and $S \in \mathcal{P}\mathfrak{F}$ where \mathfrak{F} are filters on a powerset then

$$\mathcal{A} \sqcup^{\mathfrak{F}} \bigsqcup^{\mathfrak{F}} S = \bigsqcup^{\mathfrak{F}} \langle \mathcal{A} \sqcup^{\mathfrak{F}} \rangle^* S.$$

PROOF. By theorem 380. \square

COROLLARY 458. The poset of filters on a powerset is a distributive lattice.

COROLLARY 459. The poset of filters on a powerset is a co-brouwerian lattice.

PROPOSITION 460. $a \setminus^{\mathfrak{F}} B = a \sqcap^{\mathfrak{F}} \overline{B}$ for every $a \in \mathfrak{F}$, $B \in \mathfrak{P}$ (where \mathfrak{F} is filters on a powerset and the complement is taken on \mathfrak{P}).

PROOF. By theorem 383. \square

PROPOSITION 461. Let \mathfrak{F} be the poset of filters on a powerset. $A \sqcap^{\mathfrak{F}} \bigsqcup^{\mathfrak{F}} S = \bigsqcup^{\mathfrak{F}} \langle A \sqcap^{\mathfrak{F}} \rangle^* S$ for every $A \in \mathfrak{P}$ and every set $S \in \mathcal{P}\mathfrak{F}$.

PROOF. By theorem 385. \square