

Pointfree Functors*

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Abstract

It is a part of my Algebraic General Topology research.

I generalize the point-set notion of functors to pointfree topology notion of *pointfree functors*.

In my yet unpublished research pointfree functors are used to define products of functors.

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1 Preface

This article generalizes the notions of functors introduced in [2], I call this generalization *pointfree functors*.

In my yet unpublished research pointfree functors are used to define products of functors.

2 Notation

First we use the notation introduced in [3] and [2].

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