

Proof Let denote the given funcoïd as f . $\langle f \rangle (\mathcal{I} \cup \mathcal{J}) = \langle f \rangle \mathcal{I} \cup \langle f \rangle \mathcal{J} \subseteq \mathcal{I} \cup \mathcal{J}$, $\langle f \rangle \cap S \subseteq \cap \langle \langle f \rangle \rangle S \subseteq \cap S$. Consequently the filter objects $\mathcal{I} \cup \mathcal{J}$ and $\cap S$ are closed. \square

Proposition 27 *If S is a set of filter objects closed regarding a complete funcoïd, then the filter object $\cup S$ is also closed regarding our funcoïd.*

Proof $\langle f \rangle \cup S = \cup \langle \langle f \rangle \rangle S \subseteq \cup S$ where f is the given funcoïd. \square

4 Reloids

Definition 41 *I will call a **reloid** from a small set A to a small set B a triple $(A; B; F)$ where $F \in \mathfrak{F}(A \times B)$.*

Definition 42 ***Source** and **destination** of every reloid $(A; B; F)$ are defined as*

$$\text{Src}(A; B; F) = A \quad \text{and} \quad \text{Dst}(A; B; F) = B.$$

I will denote $\text{RLD}(A; B)$ the set of reloids from A to B .

I will denote RLD the set of all reloids (for small sets).

Further we will assume that all reloids in consideration are small.

Reloids are a generalization of uniform spaces. Also reloids are generalization of binary relations (I will call a reloid $(A; B; F)$ **principal** when F is a principal filter on $A \times B$.)

I will denote $\text{up}(A; B; F) = \text{up } F$ for every reloid $(A; B; F)$.

Definition 43 *The **reverse reloid** of a reloid f is defined by the formula*

$$(A; B; F)^{-1} = (B; A; \{F^{-1} \mid F \in \text{up } f^{-1}\}).$$

Reverse reloid is a generalization of conjugate quasi-uniformity.

I will denote $\uparrow^{\text{RLD}(A; B)} f = (A; B; \uparrow^{A \times B} f)$ for every small sets A, B and a binary relation $f \subseteq A \times B$.

The order (in fact a complete lattice) on $\text{RLD}(A; B)$ is defined by the formula

$$(A; B; F) \subseteq (A; B; G) \Leftrightarrow F \subseteq G.$$

We will apply lattice operations to subsets of $\text{RLD}(A; B)$ without explicitly mentioning $\text{RLD}(A; B)$.