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Corollary 13 *A binary relation corresponds to a monovalued funcooid iff it is a function.*

Proof Because $\forall I, J \in \mathcal{P}(\text{im } f) : \langle f^{-1} \rangle^* (I \cap J) = \langle f^{-1} \rangle^* I \cap \langle f^{-1} \rangle^* J$ is true for a funcooid f corresponding to a binary relation if and only if it is a function. □

Remark 5 This corollary can be reformulated as follows: For binary relations (principal funcooids) the classic concept of monovaluedness and monovaluedness in the above defined sense of monovaluedness of a funcooid are the same.

3.14 T_0 -, T_1 - and T_2 -separable funcooids

For funcooids it can be generalized T_0 -, T_1 - and T_2 - separability. Worthwhile note that T_0 and T_2 separability is defined through T_1 separability.

Definition 37 *Let call T_1 -separable such funcooid f that for every $\alpha \in \text{Src } f$, $\beta \in \text{Dst } f$ is true*

$$\alpha \neq \beta \Rightarrow \neg(\{\alpha\} [f]^* \{\beta\}).$$

Definition 38 *Let call T_0 -separable such funcooid $f \in \text{FCD}(A; A)$ that $f \cap f^{-1}$ is T_1 -separable.*

Definition 39 *Let call T_2 -separable such funcooid f that the funcooid $f^{-1} \circ f$ is T_1 -separable.*

For symmetric transitive funcooids T_1 - and T_2 -separability are the same (see theorem 3).

Obvious 19. A funcooid f is T_2 -separable iff $\alpha \neq \beta \Rightarrow \langle f \rangle^* \{\alpha\} \asymp \langle f \rangle^* \{\beta\}$ for every $\alpha, \beta \in \text{Src } f$.

3.15 Filter objects closed regarding a funcooid

Definition 40 *Let's call **closed** regarding a funcooid $f \in \text{FCD}(A; A)$ such filter object $\mathcal{A} \in \mathfrak{F}(\text{Src } f)$ that $\langle f \rangle \mathcal{A} \subseteq \mathcal{A}$.*

This is a generalization of closedness of a set regarding an unary operation.

Proposition 26 *If \mathcal{I} and \mathcal{J} are closed (regarding some funcooid f), S is a set of closed filter objects on $\text{Src } f$, then*

1. $\mathcal{I} \cup \mathcal{J}$ is a closed filter object;
2. $\bigcap S$ is a closed filter object.