

Theorem 75 $S \subseteq B'$.

Proof Let $x \in S$. Then $Ex \in R$; $M(Ex) = E^{-1}Ex = x$; $x \in \text{im } M = B'$. \square

Obvious 24 E is a bijection from S to R .

Theorem 76 M is a bijection from B to B' .

Proof Surjectivity of M is obvious. Let's prove injectivity. Let $a, b \in B$ and $M(a) = M(b)$. Consider all cases:

$a, b \in R$ $M(a) = E^{-1}a$; $M(b) = E^{-1}b$; $E^{-1}a = E^{-1}b$; thus $a = b$ because E^{-1} is a bijection.

$a \in R, b \notin R$ $M(a) = E^{-1}a$; $M(b) = (t; b)$; $M(a) \in S$; $M(b) \notin S$. Thus $M(a) \neq M(b)$.

$a \notin R, b \in R$ Analogous,

$a, b \notin R$ $M(a) = (t; a)$; $M(b) = (t; b)$. Thus $M(a) = M(b)$ implies $a = b$.

\square

Theorem 77 $M \circ E = \text{id}_S$.

Proof Let $x \in S$. Then $Ex \in R$; $M(Ex) = E^{-1}Ex = x$. \square

Obvious 25 $E = M^{-1}|_S$.

References

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