

Conjecture 39. Let \mathcal{A} is a filter and F is a binary relation on $A \times B$ for some sets A, B .

\mathcal{A} is connected regarding $\uparrow^{\text{FCD}(A;B)}F$ iff \mathcal{A} is connected regarding $\uparrow^{\text{RLD}(A;B)}F$.

Proposition 40. The following statements are equivalent for every endofunctor μ and a set U :

1. U is connected regarding μ .
2. For every $a, b \in U$ there exists a totally ordered set $P \subseteq U$ such that $\min P = a$, $\max P = b$, and for every partition $\{X, Y\}$ of P into two sets X, Y such that $\forall x \in X, y \in Y: x < y$, we have $X [\mu]^* Y$.

Algebraic properties of S and S^*

Conjecture 41. $S(S(f)) = S(f)$ for

1. any endo-reloid f ;
2. any endo-functor f .

Conjecture 42. For any endo-reloid f

1. $S(f) \circ S(f) = S(f)$;
2. $S^*(f) \circ S^*(f) = S^*(f)$;
3. $S(f) \circ S^*(f) = S^*(f) \circ S(f) = S^*(f)$.

Conjecture 43. $S(f) \circ S(f) = S(f)$ for any endo-functor f .

Oblique products

Conjecture 44. $\mathcal{A} \times_F^{\text{RLD}} \mathcal{B} \sqsubset \mathcal{A} \times \mathcal{B}$ for some f.o. \mathcal{A}, \mathcal{B} .

A stronger conjecture:

Conjecture 45. $\mathcal{A} \times_F^{\text{RLD}} \mathcal{B} \sqsubset \mathcal{A} \times \mathcal{B} \sqsubset \mathcal{A} \times^{\text{RLD}} \mathcal{B}$ for some f.o. \mathcal{A}, \mathcal{B} . Particularly, is this formula true for $\mathcal{A} = \mathcal{B} = \Delta \cap \uparrow^{\mathbb{R}}(0; +\infty)$?

Products

Conjecture 46. Cross-composition product (for small indexed families of reloids) is a quasi-cartesian function (with injective aggregation) from the quasi-cartesian situation \mathfrak{S}_0 of reloids to the quasi-cartesian situation \mathfrak{S}_1 of pointfree functors over posets with least elements.

Remark 47. The above conjecture is unsolved even for product of two multipliers.

Conjecture 48. $a \left[\prod^{(C)} f \right] b \Leftrightarrow \forall i \in \text{dom } f: \text{Pr}_i^{\text{FCD}} a [f_i] \text{Pr}_i^{\text{FCD}} b$ for every indexed family f of functors and $a \in \text{FCD}(\lambda i \in \text{dom } f: \text{Src } f_i)$, $b \in \text{FCD}(\lambda i \in \text{dom } f: \text{Dst } f_i)$.